Quantum oscillations in the SmFeAsO parent compound and superconducting SmFeAs(O,F)

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By carrying out magnetotransport measurements up to 30 T, we succeeded in detecting and analyzing quantitatively Shubnikov-de Haas oscillations in two crystals of the *RE*FeAsO (*RE* = rare earth) family of iron pnictides, namely, the undoped SmFeAsO and the superconducting fluorine underdoped SmFeAs(O,F). We combine experimental outcomes and *ab initio* calculations of electronic structure to get the following direct evidences: (i) the Shubnikov-de Haas oscillations are determined by a two-dimensional hole band, whose effective mass is $m^* = (0.50 \pm 0.1) m_e$ in the undoped sample and $m^* = (0.89 \pm 0.1) m_e$ in the F-doped sample, while classical magnetotransport is dominated by an electron band; (ii) in the superconducting compound we give a quantitative account of the low effectiveness of electron doping associated with fluorine substitution.

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I. INTRODUCTION

Fe-based superconductors (Fe-SCs) belong to a large variety of compounds, sharing common features in terms of crystal structure, electronic structure, and magnetic ordering of the respective parent compounds. In particular, the almost nested, quasi-two-dimensional electron and hole Fermi surfaces of the parent compounds are ubiquitous and they are believed to play a crucial role in the unconventional pairing mechanism for superconductivity. In this context, extensive experimental investigation of the electronic structure of both parent and superconducting compounds across the various families of Fe-SCs is of vital importance to understand the mechanisms of high-temperature superconductivity. Specifically, Shubnikovde Haas (SdH) oscillation measurements are a powerful and straightforward probe of electronic parameters and Fermi surface topology, especially if complemented with ab initio calculations of the band structure or compared with data from other experimental techniques. Due to the availability of millimeter-size single crystals, parent compounds of the AFe_2As_2 (A = alkaline earth metal) family have been mostly studied in terms of SdH oscillations since the earliest times [1–4]. Data on superconducting members of other families are also available, namely, FeSe [5–7] and LiFeAs [8]. In the case of such superconducting samples, the large applied field must exceed the upper critical field to suppress superconductivity and allow the observation of quantum effects. In these experiments, SdH oscillations have been detected by different techniques, namely, as a magnetic-field-dependent change in the resonance frequency of a tunnel diode oscillator circuit [1-3,5], in magnetic torque experiments [8,3], or in transport measurements [4,6]. However, the agreement with band structure predicted by theory and with data from angle-resolved

photoemission spectroscopy is not always satisfying [4], and further studies would be needed in this respect. Moreover, in none of these works is the evolution of the behavior of quantum oscillations across the phase diagram spanned from the undoped parent compound towards the doped superconducting compounds ever explored. Even more importantly, on the REFeAsO (RE = rare earth) family, also called FeAs-1111 family, the one with the largest transition temperature $T_c =$ 58 K at optimal doping [9], no data of SdH oscillations have been reported so far. In Refs. [10,11], SdH oscillations have been observed on the isostructural compound LaFePO, which has been reported to be either nonsuperconducting [12] or superconducting with low $T_c \approx 6 \text{ K}$ [10,11,13]. However, this compound is nonmagnetic and does not exhibit any evidence of Fermi surface nesting or spin density wave transition; hence its behavior may not be representative in the context of nonconventional superconductivity of iron-based compounds. The reason for the difficulty in getting quantum oscillation data on the REFeAsO family is the scarce availability of single crystals that have simultaneous high-quality transport properties and size that can be handled [14].

In this work, we aim to fill two of the above-mentioned gaps in the available literature by presenting SdH oscillations from transport measurements in field up to 30 T in two single crystals of the *RE*FeAsO family, namely, undoped SmFeAsO and fluorine underdoped SmFeAs(O,F), the latter exhibiting signatures of both magnetic ordering and a superconducting transition. Our data confirm the two-dimensional character of electronic structure and the multiband scenario, both predicted by our density functional theory (DFT) calculations. Moreover, on the basis of the information on band structure and Fermi surface shape obtained from DFT calculations, we fit our SdH oscillation data in a single-band scenario and extract relevant electronic parameters for the hole band in the two samples, such as effective masses, carrier concentrations, and scattering times.

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FIG. 1. Main panels: Resistivity versus temperature curves measured in the SmFeAsO (top) and SmFeAsO_{0.96} $F_{0.04}$ (bottom) crystals. Top-left insets: SEM images of the crystals with tungsten electrical contacts; the scale bar is 10 μ m. Right insets: Hall resistance R_H versus temperature curves.

II. EXPERIMENTAL DETAILS

Our SmFeAsO and SmFeAs(O,F) single-crystal samples were prepared by flux method using CsCl as described in Ref. [15]. The in-plane (parallel to FeAs planes) crystal sizes are 5.1×9.8 and $6.8 \times 12.0 \,\mu\text{m}^2$, respectively, which is large enough to allow the fabrication of tungsten electrodes by focused ion beam (FIB) for transport measurements, as shown in the scanning electron microscope (SEM) images in the insets of Fig. 1. Magnetotransport measurements were carried out in magnetic fields up to 30 T, applied perpendicular to the sample surface (parallel to the *c* axis), and temperatures down to 380 mK. Measurements of resistivity and Hall effect up to room temperature were performed in a commercial PPMS (Physical Properties Measurement System, by Quantum Design) in fields up to 9 T.

III. RESULTS AND DISCUSSION

A. Experimental data and analysis

In Fig. 1, the temperature dependences of the resistivity and the Hall resistance of each sample are shown. The undoped sample (left) exhibits a sharp signature of the structural/magnetic transition at $T_N \approx 136$ K (calculated from the maximum of the derivative of the resistivity), below which metallic behavior is observed. The underdoped sample (right) exhibits as well a signature of the structural/magnetic transition, whose sharpness points to the high quality of the sample but at a smaller temperature $T_N \approx 127$ K, and a high-temperature resistivity value smaller by a factor of 2. A superconducting transition is seen at $T_c \approx 6$ K (calculated at the onset of the resistivity drop, while the zero resistivity state is not completely reached even at the lowest measuring temperatures). This superconducting phase lies in the underdoped regime and has an upper critical field $\mu_0 H_{c2} \approx 12 \,\mathrm{T}$ at 0.3 K, as estimated from the change of concavity in the resistance versus field curve (see Supplemental Material [16] for details). The coherence length, which can be extracted as $\xi_0 = \sqrt{\Phi_0/2\pi\mu_0 H_{c2}} \approx 5 \,\text{nm}$, is in trend with values of $\xi_0 \approx 3 \text{ nm}$ for $T_c = 33 \text{ K}$ and $\xi_0 \approx 2 \text{ nm}$ for $T_c = 52 \text{ K}$ [17]. This suggests the bulk nature of superconductivity. For a comparison of the effect of nominal fluorine doping of 4% on T_N and T_c as extracted from transport measurements, we note that available literature phase diagrams are all built from data on polycrystalline samples and show somewhat scattered values of T_N and T_c as a function of fluorine doping [18–21]. Thus they may not be an ideal reference to our case; however, our data are in fair agreement with Ref. [18].

The magnitude of the upper critical field, $H_{c2} \approx 12 \,\mathrm{T}$ at 0.3 K (see Supplemental Material [16] for details), is small enough to be suppressed by the applied field, allowing quantum oscillation measurements. The temperature dependence of the Hall resistance R_H , also shown in Fig. 1, indicates that for both samples the structural/magnetic transition triggers a condensation of charge carriers, likely related to the opening of a spin density wave gap, determining an increase in the magnitude of R_H down to low temperatures. At low temperatures, the negative sign of R_H indicates that an electron-type band dominates transport in both samples, and the smaller magnitude of R_H in the doped sample is consistent with the introduction of *n*-type carriers by fluorine doping. In the higher temperature regime above T_N , R_H changes from values around $-1 \times 10^{-9} \text{ m}^3/\text{C}$ in the undoped sample to values around $-3 \times 10^{-9} \text{ m}^3/\text{C}$ in the doped sample. Possibly, the effect of *n*-type doping in this temperature range can be seen as a departure from electron-hole compensation towards electron predominance.

Magnetoresistance measurements were performed up to 30 T with field perpendicular and parallel to the FeAs plane. (Raw magnetoresistance data are presented in the Supplemental Material [16].) SdH oscillations are only observed in perpendicular field, which points to the two-dimensional character of the Fermi surface in these compounds. In contrast, in 122 parent compounds, quantum oscillations have been observed also in parallel field [2–4], indicating a more threedimensional character. To evidence oscillations, from our raw magnetoresistance data, a nonoscillating magnetoresistance background of the form $\rho_{bg}(B) = \rho_0 + \rho_1 B + \rho_2 B$ [2] was subtracted, where ρ_1 and ρ_2 are fitting constants representing the linear Abrikosov quantum magnetoresistivity and quadratic cyclotronic magnetoresistivity.

In Fig. 2, we present two sets of SdH magnetoresistance oscillations $\Delta \rho = (\rho - \rho_{\text{bg}})/\rho_0$ measured at different temperatures in the two samples. As expected, the amplitude of the oscillations is exponentially damped with increasing temperature and with increasing inverse field 1/B, as predicted by the Lifshitz-Kosevic (L-K) formalism [22], described in the Supplemental Material [16]. We first analyzed our experimental curves by performing the fast Fourier transform (FFT). The results for the undoped and the doped samples are shown in the insets of Figs. 3(a) and 3(b), respectively: in both



FIG. 2. Normalized magnetoresistivity versus inverse field (bottom axis) curves measured in the SmFeAsO (top) and SmFeAsO_{0.96} $F_{0.04}$ (bottom) crystals. In particular, the nonoscillating background magnetoresistance ρ_{bg} is subtracted from the raw resistivity data ρ and the result is normalized to the zero field resistivity ρ_0 .

cases a main peak centered at a frequency $F_B = (65 \pm 6)$ T is found. According to the relationship $F_B = 2e/hn_{2D}$, where *h* is the Plank constant, *e* the electron charge, and n_{2D} the two-dimensional carrier concentration $(n = n_{2D}/c)$, with *c* the out-of-plane lattice parameter), these frequencies correspond to volume carrier concentrations $n = (3.9 \pm 0.3) \times 10^{25} \text{ m}^{-3}$.

In addition, we obtain the effective masses m^* of carriers in these bands associated to the frequency F_B , by fitting the temperature evolution of the FFT peak amplitudes with the function $\chi/\sinh(\chi)$, where $\chi = 2\pi^2 k_{\rm B} m^* T/(eB)$, and $k_{\rm B}$ is the Boltzmann constant. The outcomes of this analysis are $m^* = (0.50 \pm 0.1) m_e$ and $m^* = (0.89 \pm 0.1) m_e$ for the undoped and doped samples, respectively.

Since only one main frequency can be extracted from our SdH oscillations, we fit the experimental data with the complete L-K formula at T = 0.4 K using the FFT frequency as a fixed input parameter. As shown in Fig. 4, we obtain a very good agreement between the data and the model. This fitting procedure gives as output parameters both the effective masses m^* and the scattering times τ . In particular, for the parent compound SmFeAsO we obtain $m^* = 0.53 m_e$ and $\tau = 1.21 \times 10^{-13}$ s, while for the doped sample SmFeAsO_{0.96}F_{0.04} we obtain $m^* = 1.00 m_e$ and $\tau = 1.53 \times 10^{-13}$ s. The effective masses extracted from the fit with the complete L-K formula are pretty consistent with the values obtained from the analysis of temperature dependence of the FFT peak.

B. Theoretical calculations

We now turn to the results of DFT calculations. DFT calculations are performed in the antiferromagnetic state (see Supplemental Material for details [16]). In Fig. 5 (inset) we show a perspective view of the Fermi surface (FS), with one hole sheet (red) and two electron sheets (blue). The hole FS is a nearly perfect cylinder with negligible dispersion along k_z . The electron FSs are two weakly bent cylinders with a slightly elliptical cross section. The shape of both hole and electron FSs is in good agreement with DFT calculations performed in Ref. [23] on LaFeAsO. The ratio of the areas of the two extremal cross sections is close to unity, 1.4 and 1.7 for the holes and electrons, respectively, confirming their almost cylindrical nature. Stoichiometric SmFeAsO is a perfectly compensated semimetal. Our calculations confirm this finding. Indeed, the volume inside each electron FS is exactly one-half of the corresponding volume of the hole FS. The compensated nature of SmFeAsO, together with the 2D dispersion of the bands at E_F , brings us to the important result that the average cross-sectional area of the electron FS must be half of the corresponding one for the hole. This latter result is valid only for the undoped compound. Upon F doping, the balance of electrons and holes is broken and electrons are added into the system. Given the low doping concentrations studied here, we use a rigid-band approach to simulate the effect of F doping on the FS's shapes and sizes. In Fig. 5, we show a plot of the calculated oscillation frequencies F_B as a function of electron doping in SmFeAsO. We see that for the undoped compound, F_B values are 30 and 60 T for electrons and holes, respectively. Remarkably, the frequency associated to holes corresponds to our experimental values extracted from quantum oscillations in both the undoped and doped samples, which makes it plausible to associate the experimental quantum oscillations to this hole band.



FIG. 3. Temperature evolution of the FFT peak amplitudes for the SmFeAsO (a) and SmFeAsO_{0.96} $F_{0.04}$ (b) crystals. Continuous lines are fitting functions (see text).



FIG. 4. Oscillating magnetoresistivity versus field curves measured in the SmFeAsO_{1-x} F_x with x = 0 (top) and x = 0.04 (bottom) crystals. Single-band L-K fittings are shown as continuous lines.

DFT calculations indicate the existence of two types of carriers whose densities should be balanced in the undoped sample. The multiband description is also necessary to account for the behavior of the Hall effect data (insets of Fig. 1), whose temperature dependence is not compatible with a single-band scenario [24]. Moreover, the Hall coefficient is negative at low temperature, suggesting that it is dominated by an electron band, opposite to SdH oscillations that we associate to the hole band. In order to account for this phenomenology, we can simply consider the two-band model for the Hall coefficient $R_h = (n_h \mu_h^2 - n_e \mu_e^2)/[e(n_e \mu_e + n_h \mu_h)^2],$ where $n_{e/h}$ and $\mu_{e/h}$ are the electron/hole densities and mobilities, respectively. If we assume $n_e = n_h$ for the undoped sample, according to the compensation predicted by DFT calculations, it is straightforwardly seen that any μ_e larger than μ_h yields a negative Hall coefficient. Moreover, if we use the scattering time and the effective mass of the



FIG. 5. Main panel: Computed value for the SdH oscillation frequency as a function of doping (blue for electrons and red for holes). Positive values correspond to n-type doping. On the right Y axis the cross-section areas are given. Inset: View of the Fermi surfaces of SmFeAsO inside the first Brillouin zone of the four formula unit cell.

hole band obtained from quantum oscillations to evaluate the hole mobility μ_h and we assume the same *n* value for both the bands as obtained from the oscillation frequencies, we find that the so-calculated R_h well approximates the experimental value of low-temperature Hall coefficient in the limit $\mu_e \gg \mu_h$, where $R_h \approx (-en_e)^{-1} = -(1.6 \pm 0.2) \times 10^{-7} \text{ m}^3/\text{C}$. Hence, by combining our measurements with DFT calculations, we obtain that a high-mobility electron band should exist to explain transport measurements. Remarkably, this finding agrees with the presence of high-mobility electron-type Dirac cones in the band structures of these parent compounds, predicted by our ab initio calculations (see Supplemental Material [16] for details), and also theoretically predicted and confirmed by other experimental techniques in literature both in 1111 [25,26] and in 122 [27] families. According to calculations, these linear dispersing bands are associated to cylindrical electronic FS, whose cross section is around half of the hole FS (see inset of Fig. 5). This implies that the period of the oscillations should be twice as much as the period of the hole band, which requires higher magnetic fields than those reached in this experiment to be unambiguously detected.

Let us now turn our attention to the doped sample. According to DFT calculations, in the rigid-band approach, the doping increases (decreases) the electron (hole) F_B , so that above a 2.3×10^{25} m⁻³ electron doping concentration, the electrons should have a frequency higher than that of the holes (see Fig. 5). On the contrary, the frequency of the quantum oscillations that we observe in the doped sample is almost the same as that of the parent compound, as if the carrier density of the hole band was not affected by the substitution. Hence, we gather that F substitution is less effective than what is predicted by the application of the rigid-band model to the band structure obtained by DFT calculations. The explanation for this seeming discrepancy between theory and experiment is that F does not behave as a shallow donor but it is actually a deep impurity. Hence, the band structure is altered by the introduction of F impurities across a wide spectrum of energies, so that on one hand the rigid-band approximation still works, because in proximity of the Fermi level the band changes are not significant, and on the other hand the change in the band filling is less than nominal, that is, less than one electron per F. This scenario is confirmed by band structure calculations on the SmFeAsF compound (see Supplemental Material [16] for details).

IV. CONCLUSIONS

In conclusion, we measured the magnetotransport properties of two high-quality SmFeAsO_{1-x} F_x (x = 0; 0.04) single crystals of several microns size, in magnetic fields up to 30 T and temperatures down to 380 mK. Two-dimensional Shubnikov-de Haas oscillations are observed in both samples, remarkably also in the superconducting fluorine underdoped sample ($T_c = 6$ K) for fields above 16 T well exceeding the upper critical field. We analyze quantitatively the SdH oscillation curves within the L-K formalism. From the comparison with our *ab initio* calculations of electronic structure and Fermi surfaces, we identify the oscillating band with the hole sheet of the Fermi surface for both samples. By fitting the temperature dependence of the oscillation amplitudes, we extract effective mass values $m^* = (0.50 \pm 0.1) m_e$ and $m^* = (0.89 \pm 0.1) m_e$ for the undoped and doped samples, respectively. The comparison of oscillation frequencies and low-temperature Hall effect data in the two samples suggest that F substitution is significantly less effective than what is predicted by DFT calculations in terms of band filling. This evidence of the low effectiveness of fluorine doping establishes the correct scale along the doping axis of the phase diagram of these compounds.

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